- 1. A long bar of rectangular cross section is 60 mm by 90 mm on a side and has thermal conductivity of 1 W/m °C. One surface is exposed to a convection process with air at 100°C and a convection coefficient T_{π} of 100 W/m²°C, while the remaining surfaces are maintained at 50°C. Using a grid spacing of 30 mm and the Gauss-Seidel method, determine the nodal temperatures and the heat rate per unit length normal to the page into the bar from the air.
- 2. Consider the two dimensional grid ($\Delta x = \Delta y$) representing steady state conditions with no internal volumetric generation for a system with thermal conductivity k. One of the boundaries is maintained at a constant temperature T_s while the others are adiabatic. Derive an expression for the heat rate per unit length normal to the page crossing the isothermal boundary (T_s) .
- 3. Consider the square channel shown in the sketch operating under steady state conditions. The inner surface of the channel is at a uniform temperature of 600 K, while the outer surface is exposed to convection with a fluid at 300 K and a convection coefficient of 50 W/m² °C. From a symmetrical element of the channel, a two dimensional grid has been constructed and the nodes labeled. The temperatures for nodes 1, 3, 6, 8 and 9 are identified.
 - a) Determine the temperature T_2 , T_4 and T_7 .
 - b) Calculate the heat loss per unit length of the channel.





 $\Delta x = \Delta y = 0.01 \text{ m}$ T₁ = 430 K T₆ = 492 K k = 1 W/m °C $T_2 = 394 \text{ K}$ $T_8 = T_9 = 600 \text{ K}$



Δx

٥.

Isothermal

Insulation

12•

13.

14.

11.

3.

2.

10

The steady state temperatures (°C) associated with selected nodal of a two dimensional system having a thermal conductivity of 1.5 W/m°C are shown on the accompanying grid.

a) Determine the temperature at nodes 1,2

- b) Calculate the heat transfer rate per unit thickness normal to the page from the system to the fluid.
- 5. A steady state, finite difference analysis has been performed on a cylindrical fin with a diameter of 12 mm and a thermal conductivity of 15 W/m°C. The convection process is characterized by a fluid

Insulated 0.1 m boundary 45.8 129.4 0.1 m T_∞ = 30°C T_2 137 103.5 $h = 50 W/m^{2}$ °C 67 172.9 T, 132.8 Isothermal boundary $T_0 = 200^{\circ}C$



temperature of 25°C and a heat transfer coefficient of 25 W/m²°C.

- a) The temperature for the first three nodes separated by a spatial increment of $\Delta x = 10$ mm, are given in the sketch. Determine the fin heat rate.
- b) Determine the temperature at node 3, T₃.